



New collective mode in $\text{YBa}_2\text{Cu}_3\text{O}_{6+x}$ observed by time-domain reflectometry

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We report the observation of coherent oscillations associated with charge-density-wave (CDW) order in the underdoped cuprate superconductor $\text{YBa}_2\text{Cu}_3\text{O}_{6+x}$ by time-resolved optical reflectivity. Oscillations with frequency 1.87 THz onset at approximately 105 and 130 K for dopings of $x = 0.67$ (ortho-VIII) and $x = 0.75$ (ortho-III), respectively. Upon cooling below the superconducting critical temperature (T_c), the oscillation amplitude is enhanced, the phase shifts by π , and the frequency softens by $\delta\nu/\nu \approx 7\%$. A biquadratically coupled Landau-Ginzburg model qualitatively describes this behavior as arising from competition between superconducting and CDW orders.

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The concept of spontaneous symmetry breaking (SSB) constitutes a paradigm in many branches of physics, most especially high-energy particle phenomenology, and yet has its roots in the study of condensed matter.¹⁻³ In metals characterized by strongly-interacting electrons, breaking of U(1) gauge symmetry leads to superconductivity (SC), and breaking of translation and time-reversal symmetry correspond to the formation of charge- and spin-density waves. New phenomena may be anticipated in metals in which charge-density waves (CDWs) and SC coexist and interact strongly, such as the coupling of their respective collective modes and possible detection of the SC amplitude mode,⁴⁻⁶ the condensed matter analog of the Higgs boson.

Recently, great interest has been generated by the observation, using resonant⁷⁻⁹ and hard^{10,11} x-ray scattering, of a CDW coexisting with SC in underdoped crystals of the prototypical high- T_c cuprate superconductor, $\text{YBa}_2\text{Cu}_3\text{O}_{6+x}$ (YBCO). Particularly relevant is the finding that the CDW amplitude increases initially as the temperature (T) is lowered but then decreases as T crosses T_c , indicating a repulsive interaction between SC and CDW phases. These discoveries raise key questions concerning the relation of the newly found CDW in YBCO to the coupled charge and spin (stripe) order in $\text{La}_{2-x}(\text{Sr}, \text{Ba})_x\text{CuO}_4$ and related systems,^{12,13} other phenomena that onset in a similar range of $T > T_c$, such as fluctuating SC,^{14,15} anomalies in transient reflectivity, Hall and Kerr effects,¹⁶⁻¹⁸ and the opening of the pseudogap itself.

In this work, we report the observation by time-domain reflectometry of a new collective mode in YBCO crystals in which the CDW order was previously detected. On the basis of the approximate coincidence of the onset T of the transient reflectivity signal and x-ray scattering, we associate the new mode with the presence of CDW order. From analysis of the time-domain data, we obtain the T dependence of the amplitude, frequency, phase, and damping parameter of the mode. We observe clear anomalies in these parameters as T is lowered in the SC state, providing information concerning the nature of the coupling between the two coexisting forms of order.

Time-resolved measurements of the photoinduced change in optical reflectivity, ΔR , were performed using a mode-locked Ti:sapphire oscillator generating pulses of 800-nm wavelength light of duration 60 fs and repetition rate 80 MHz. Measurements were carried out using both the conventional two-beam pump/probe approach and a four-beam transient grating (TGS) configuration.^{19,20} All measurements reported in this paper were performed using a pump fluence of $1.5 \mu\text{J}/\text{cm}^2$. Single crystals of YBCO ortho-VIII, with $x = 0.67$, hole doping $p = 0.12$, and $T_c = 67$ K, and ortho-III, with $x = 0.75$, $p = 0.13$, and $T_c = 75$ K, were studied. By comparing measurements under photoexcitation with thermodynamic and transport measurements, we estimate an average laser heating of 5 K in the vicinity of T_c .

Figures 1(a)–1(c) present results for $\Delta R(t)$ normalized by the equilibrium reflectance R in a crystal of YBCO ortho-VIII, measured using the two-beam configuration. Figure 1(a) illustrates the pronounced anisotropy of the response in the crystallographic a - b plane, with ΔR changing sign as the probe polarization is rotated from the a to the b axis, while the pump polarization is held parallel to the a axis (the crystallographic axes were oriented by x-ray Laue diffraction to within 5°). An oscillating reflectivity modulation is clearly present in both polarization channels and is highlighted using the expanded scale in Fig. 1(b). In order to quantify the parameters of the oscillation, we subtract a background function of the form $Ae^{t/\tau_1} + Be^{-t/\tau_2} + C$ from each $\Delta R(t)/R$ curve to obtain the oscillating component ΔR_Ω . The resulting difference transient is shown for $T = 5$ K in Fig. 1(b) and for a series of temperatures between 5 and 120 K in Fig. 1(c).

Figure 2(a) shows the T dependence of the oscillation amplitude $A_\Omega(T)$ as extracted from the data shown in Fig. 1(c). To obtain $A_\Omega(T)$ we first Fourier transform $\Delta R_\Omega(t)$ to obtain the spectral density function $|\Delta R_\Omega(\nu)|^2$ and fit it to a damped harmonic oscillator response function. The spectrum at 5 K and the best fit are shown in the inset in Fig. 2(a). We observe that the temperature dependence of $A_\Omega(T)$ extrapolates to 0 at an onset temperature $T \approx 105$ K, with oscillations clearly observable above the noise level at $T \approx 90$ K. $A_\Omega(T)$

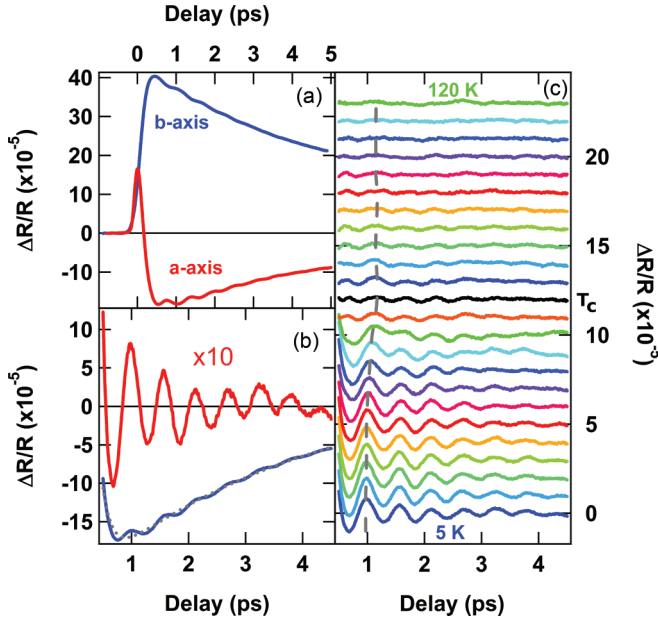


FIG. 1. (Color online) (a) $\Delta R(t)/R$ for $x = 0.67$ at 15 K with the probe beam polarized parallel to the crystallographic a axis (red curve) and b axis (blue curve). Oscillations are present in both polarization channels. (b) a -axis $\Delta R(t)/R$ at 5 K [lower (blue) curve] with the fit to the nonoscillating background [dashed (gray) curve] and the subtracted oscillating component ΔR_Ω [upper (red) curve]. (c) T dependence of ΔR_Ω , shown in 5 K steps between 5 and 120 K. The first maxima are shown by the vertical dashed (gray) curve, and the curve nearest T_c is plotted in black.

then begins to increase much more rapidly upon cooling below T_c .

Next, we compare $A_\Omega(T)$ with the temperature dependence of the nonoscillatory component of ΔR . The pump-probe reflectivity dynamics of YBCO are similar to those in other cuprate superconductors;^{21–27} a rapidly decaying transient is observed in the normal state, which persists into the superconducting (SC) state, and a larger and longer-lived response appears below T_c . The existence of multiple components below T_c is especially clear in the a -axis transient shown in Fig. 1(a), where the two components of ΔR have opposite signs. The component of ΔR that appears at or near T_c is associated with the ultrafast photoinduced evaporation of a fraction of the superfluid condensate and its subsequent reformation.^{28–30} The transient that is observed in the normal state is more complicated, consisting typically of at least two components: a nearly T independent bolometric signal associated with photoinduced heating of the electron gas and another component that appears at or below the pseudogap temperature T^* .^{16,26}

We have found that performing time-domain reflectivity in the four-beam TGS mode is very useful in helping to distinguish the several contributions to ΔR (smooth background and oscillatory) on the basis of their optical phase. In TGS, the reflected probe pulse is coherently mixed with a local oscillator pulse with an adjustable optical phase, allowing direct measurement of both the amplitude and the phase of the photoinduced change in the complex reflection amplitude, $\delta\tilde{r}$.³¹ Traditional pump-probe reflectivity cannot

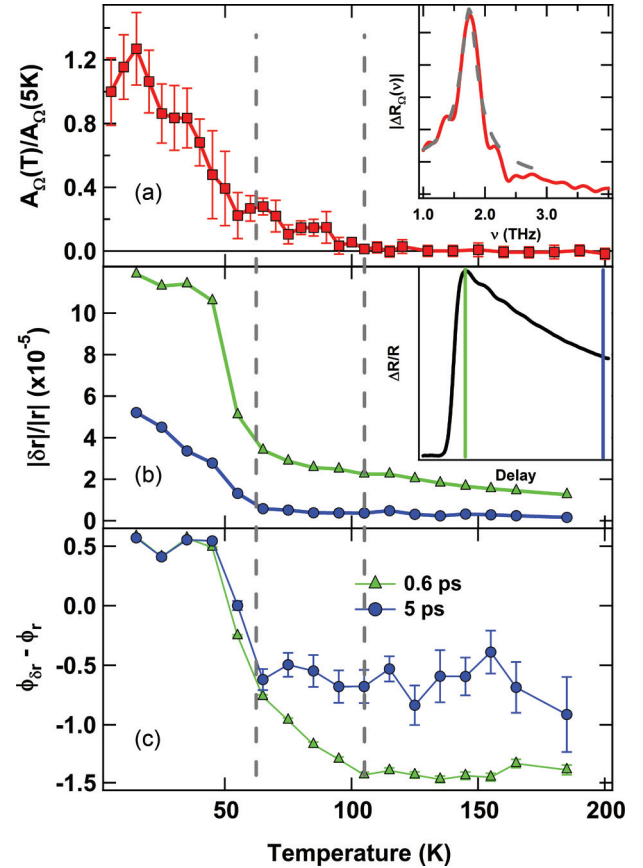


FIG. 2. (Color online) (a) The T dependence of the oscillation amplitude extracted from the Fourier transforms of the $x = 0.67$ data in Fig. 1(c). Inset in (a): $\Delta R_\Omega(\nu)$ at 5 K, with the fit shown by the dashed (gray) curve. The T dependence of (b) the amplitude and (c) the phase of the a -axis TGS signal at probe delays of 0.6 and 5 ps, marked on a representative $\Delta R(t)/R$ curve in the inset in (b). The amplitude increases sharply at T_c for all time delays, indicating the onset of the SC response. A phase rotation at 0.6 ps onsets at 105 K, while remaining constant in the normal state at 5 ps. Note the dashed vertical lines indicating the onset of oscillations at 105 K and the enhancement at T_c , corresponding to the two onset temperatures observed in the TGS dynamics.

directly measure the phase of $\delta\tilde{r}$, measuring only $\Delta R/R$, where $R + \Delta R = |\tilde{r} + \delta\tilde{r}|^2$. When applied to YBCO, TGS reveals that, despite the appearance of ΔR in Fig. 1(a), the nonoscillatory components of the transient reflectivity $\delta\tilde{r}_a$ and $\delta\tilde{r}_b$ are identical, with the apparent anisotropy coming entirely from a phase difference between \tilde{r}_a and \tilde{r}_b . However, analysis of the TGS data indicates that the oscillatory components do display some anisotropy; the ratio of the oscillatory to the background components of $\delta\tilde{r}$ is $35\% \pm 18\%$ higher along a than along b . Finally, TGS shows that the oscillations are not a modulation of the background $\delta\tilde{r}$, since the two components of the signal have distinct optical phases, by 0.3π .

In Figs. 2(b) and 2(c) we plot the amplitude and optical phase (relative to \tilde{r}_a), respectively, of $\delta\tilde{r}_a$ as a function of T , for two representative time delays. The amplitude, $|\delta\tilde{r}|$, increases sharply at T_c for both delays, in a manner that appears to be correlated with the amplitude of the oscillation. Above T_c , $|\delta\tilde{r}|$ displays a weak and featureless T dependence, persisting

above 200 K. Despite the smooth T dependence of the $\delta\tilde{r}$ amplitude, the phase [Fig. 2(c)] shows structure upon cooling below 105 K, the same T at which the reflectivity oscillations become observable. At this point we cannot tell whether this feature in the phase of $\delta\tilde{r}$ reflects the onset of CDW order or phase-fluctuating SC.

The most striking aspect of the data plotted in Fig. 2 is the enhancement $A_\Omega(T)$ correlated with the onset of SC. The result is surprising given the direct observation by x-ray scattering of the reduction of the CDW amplitude with the appearance of SC in the same material.¹⁰ Since we associate ΔR_Ω with the onset of CDW order, it would be natural to expect a suppression of the collective mode due to competition with SC. Below we show how this seemingly anomalous behavior can emerge as a consequence of SC-CDW coupling.

A simple description of coupled order parameters is given by the Ginzburg-Landau free energy,¹⁰

$$\mathcal{F}(\Phi, \Psi) = -a|\Phi|^2 + \frac{b}{2}|\Phi|^4 - \alpha|\Psi|^2 + \frac{\beta}{2}|\Psi|^4 + \lambda|\Phi|^2|\Psi|^2, \quad (1)$$

where Φ and Ψ are the CDW and SC order parameters, respectively, and λ is a constant representing the strength of coupling between the two. For the case of coexisting orders with a repulsive interaction, the parameters a , α , and λ are all positive. Minimizing the free energy with respect to $|\Phi|$ yields, for the equilibrium value of the CDW order parameter,

$$|\Phi_{\text{eq}}|^2 = \frac{a - \lambda|\Psi|^2}{b}, \quad (2)$$

showing that, for a repulsive interaction between the two orders, the CDW amplitude is suppressed in the presence of SC order.

Figure 3(a) shows how the repulsive interaction between the two order parameters provides a mechanism for photoexcitation of the CDW-related mode in the SC state. The lower part of this figure ($T < T_c$) is a plot of the free energy as a function of the CDW order parameter for two values of the SC amplitude. The curve with the lowest free energy corresponds to the equilibrium value of Ψ , while the curve above it is calculated using a smaller value of Ψ . As expected from the repulsive interaction between the two orders, the CDW amplitude is higher in the state with weaker SC. As illustrated in Fig. 3(a) by the directed laser pulse, the effect of photoexcitation is to impulsively reduce the SC order, inducing a transition from the lower to the upper free energy curves. The sudden shift in the value of $|\Phi|$ that minimizes the free energy drives the oscillation of the CDW amplitude.

The initial amplitude of the ensuing oscillation is the shift in the minimum of Φ that accompanies photoexcitation, which, to first order in λ , is equal to

$$\delta|\Phi| = |\Phi_0| \frac{\lambda}{2a} \delta|\Psi|^2 \propto |\Psi|^2, \quad (3)$$

where Φ_0 is the equilibrium value CDW order in the absence of coupling to SC. The proportionality to $|\Psi|^2$ on the right-hand side of Eq. (3) follows from the previous demonstration³⁰ that, for all temperatures below T_c , the photoinduced decrease in SC order for a fixed laser fluence is proportional to $|\Psi|^2$ itself. This simple calculation reproduces the counter-intuitive result that

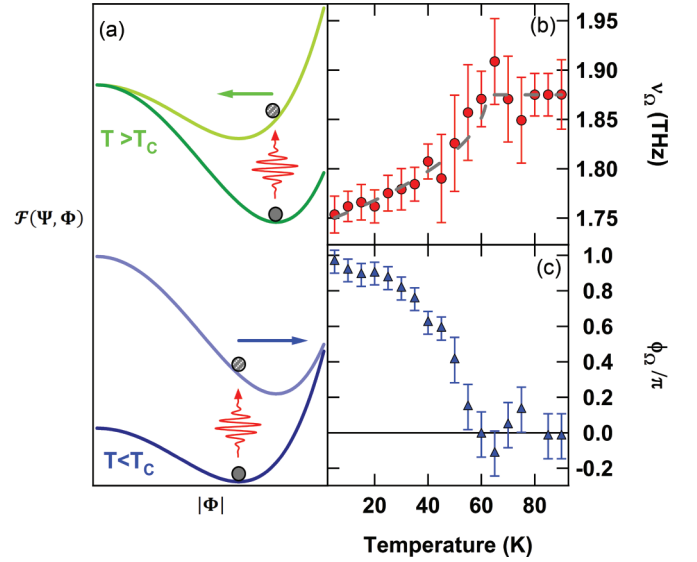


FIG. 3. (Color online) (a) Schematic of the displacive excitation mechanism described in the text. Below T_c , pump excitation raises the free energy via partial evaporation of the SC condensate, decreasing the SC order parameter $|\Psi|$. This leads to an increase in the quasiequilibrium value of the CDW order parameter $|\Phi|$, as represented in the lower half of (a). Above T_c , the free energy increases via direct photosuppression of CDW order, leading to a reversal of the initial displacement of the free energy minimum. T dependence of (b) the frequency and (c) the phase of the CDW oscillations. The dashed (gray) line in (b) gives the fit to $\nu_\Omega(T)$ obtained from the coupled Ginzburg-Landau model.

the amplitude of the CDW oscillations is proportional to $|\Psi|^2$ and, therefore, is enhanced by SC, even as $|\Phi_{\text{eq}}|$ is suppressed.

The T dependence of the oscillation frequency ν_Ω obtained from the fits to $\Delta R_\Omega(\nu)$ is plotted in Fig. 3(b). The frequency in the normal state, 1.87 THz (62 cm^{-1}), is well below that of the lowest optic phonon in the YBCO system, which is a Ba-O mode whose frequency is $\approx 120 \text{ cm}^{-1}$, as measured both by both Raman³² and by time-domain reflection spectroscopies.^{33–35} As Fig. 3(b) shows, ν_Ω begins to decrease with the appearance of SC order, accompanied by a decrease in the damping time from $1.9 \pm 0.5 \text{ ps}$ averaged over $T > T_c$ to $1.3 \pm 0.2 \text{ ps}$ for $T < T_c$, further evidence of a picture of coupled order parameters. Softening of the restoring force of the oscillation is expected from the curvature of \mathcal{F} evaluated at equilibrium value of CDW order,

$$\left. \frac{\partial^2 \mathcal{F}}{\partial |\Phi|^2} \right|_{\text{eq}} = 4(a - \lambda|\Psi|^2). \quad (4)$$

The dashed (gray) curve through the data points in Fig. 3(b) is a fit to Eq. (4) assuming an approximately BCS-like, temperature-dependent SC order parameter $|\Psi|^2(T) \propto (1 - T^2/T_c^2)^{1/2}$.

Another clear, and yet unexpected, feature of the T dependence of the collective mode parameters is the shift in the phase ϕ_Ω of the oscillations upon entering the SC state, as shown in Fig. 3(c) (note that this phase is different from the optical phase of the reflectivity amplitude discussed above). The phase shift is apparent from the time-domain oscillations

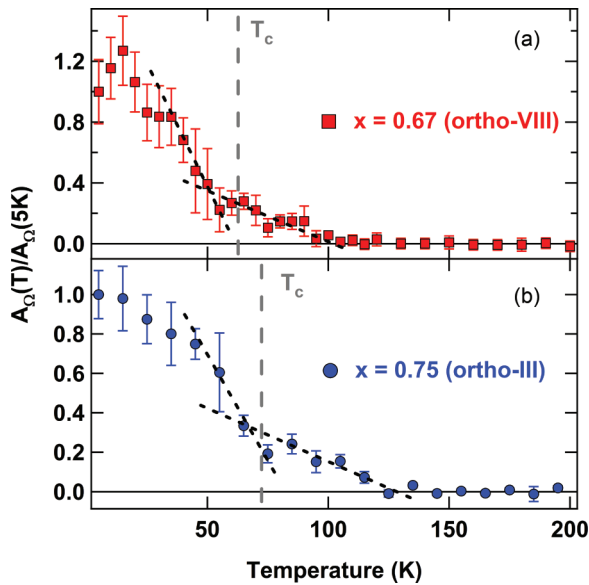


FIG. 4. (Color online) T dependence of CDW oscillations for (a) $x = 0.67$ (ortho-VIII) and (b) $x = 0.75$ (ortho-III). The dashed (black) lines are guides for the eye. Oscillations initially onset at approximately 105 K in ortho-VIII and 130 K in ortho-III, with both dopings displaying a pronounced enhancement in oscillation amplitude at T_c .

plotted in Fig. 1(c), where the dashed vertical line traces out the delay time of the first crest of the oscillation as a function of T . As indicated in Fig. 3(c), the total phase difference from $T > T_c$ to low temperatures is quite close to π . To explain this effect, we consider the excitation mechanism of the CDW oscillation in the normal state. In the absence of a competing SC state, pumping is expected to weaken the CDW order.^{36–38} This corresponds to a decrease in the quasiequilibrium value of $|\Phi|$, as shown in the upper part of Fig. 3(a), where we plot \mathcal{F} as a function of $|\Phi|$ in equilibrium (lower curve) and after photoexcitation (upper curve). As the horizontal arrows indicate, the sign of the initial displacement above T_c is opposite to that predicted in the SC state, in agreement with our observation of a π phase shift.

In addition to the measurements reported above, we have observed and characterized the collective mode oscillations in YBCO ortho-III, in which CDW ordering has also been observed. In Fig. 4 we compare the amplitude of the oscillations in the two compounds that we have studied thus far. Overall, the behavior of $A_Q(T)$ is qualitatively the same - onset in the normal state and rapid increase for $T < T_c$ - although in YBCO ortho-III the onset of the oscillations extrapolates to a higher $T \approx 130$ K. In addition, in the ortho-III compound we have found the same shift in phase

and reduction in frequency upon entering the superconducting state as shown for the ortho-VIII sample in Fig. 3.

By way of conclusion, we address some of the questions raised by our observations and their implications for future research. The first such question is whether the mode we have observed is, in fact, the amplitude mode of the CDW. On the basis of the measured frequency of 60 cm^{-1} , we can rule out phonon modes of the structure above the CDW ordering temperature, T_{CDW} . The fact that the new mode appears only at $T < T_{CDW}$ strongly suggests that it is correlated with symmetry breaking in a low- T phase. However, the parameters of the oscillation do not show some of the signatures expected for an amplitude mode. At the level of mean-field theory, the frequency of the amplitude mode should go to 0 as T approaches the CDW ordering temperature, T_{CDW} . Although in real CDW systems the frequency does not shift all the way to 0, the mode is found to soften considerably and become overdamped as $T \rightarrow T_{CDW}$.^{38,39} By contrast, the frequency and damping parameters that we observe remain constant even as the amplitude of the mode vanishes with increasing T . This apparent discrepancy raises the possibility that the new mode originates as an acoustic phonon whose wave vector matches that of the CDW. Once the CDW distortion takes place this mode will be shifted to zero wave vector and become observable by optical probes.⁴⁰

A second, and closely related, question is the relation of the new mode in YBCO to low-frequency collective modes observed in the $\text{La}_{2-x}(\text{Sr}_x\text{Ba}_x)\text{CuO}_4$ family of cuprates. In particular, the mode frequency ($\nu \approx 2.0 \text{ THz}$) and T -dependent amplitude recently reported³⁶ in thin films of $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ (LSCO) are strikingly similar to what we observe in the YBCO crystals, although the damping time is roughly five times shorter. The similarity is surprising in that scattering probes suggest very different CDW structures in the two compounds: stripe-like coupled spin and charge fluctuations in LSCO,^{12,13} as opposed to CDWs uncorrelated with spin fluctuations, perhaps with a two-dimensional checkerboard structure, in YBCO.⁷ However, the similarity might be explained if the collective modes in both systems result from mixing-down of acoustic modes to zero wave vector, rather than CDW amplitude modes. We believe that, regardless of what ultimately proves to be their origin, careful study of these new collective modes as a function of temperature, doping, and magnetic field will contribute greatly to our understanding of the role of CDW and SC coupling in the cuprate family of superconductors.

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