I. INTRODUCTION

There is increasing interest in dynamic control of magnetism in ferromagnets. Of particular interest are the related questions of how quickly and by what mechanism the magnetization can be changed by external perturbations. In addition to advancing our basic understanding of magnetism, exploring the speed with which the magnetic state can be changed is crucial to applications such as ultrafast laser-writing techniques. Despite its relevance, the time scale could occur on time scales significantly less than 1 ps. Since then demagnetization has usually been attributed to Elliott-Yafet mechanism, in which the rate of electron spin flip is proportional to the momentum scattering rate. Recently Koopmans et al. have demonstrated that electron-phonon or electron-impurity scattering can be responsible for the wide range of demagnetization time scales observed in different materials. Also, recently it has been proposed that electron-electron scattering should be included, as well as a source of Elliott-Yafet spin flipping and, consequently, demagnetization. Although Ref. 5 specifically refers to interband scattering at high energies, it is plausible that intraband electron scattering can lead to spin memory loss as well.

Time-resolved magneto-optical Kerr effect (TRMOKE) measurements have been demonstrated to be a useful probe of ultrafast laser-induced demagnetization. In this paper we report TRMOKE measurements on thin films of SRO grown on (111)-oriented SrTiO$_3$ (STO) substrates at between 5 and 165 K. Below about 80 K we observe damped ferromagnetic resonance (FMR), from which we determine a Gilbert damping parameter consistent with earlier measurements on SrTiO$_3$ with a (001) orientation. As the Curie temperature (~150 K) is approached the demagnetization time slows significantly, as has been observed in other magnetic systems. The slowing dynamics have been attributed to critical slowing-down, due to the similarities in temperature dependency between the demagnetization time and the relaxation time. In this paper we develop an analytical expression relating the demagnetization time to the spin-flip time near the Curie temperature. This provides a new method of measuring the spin-flip time, which is essential to understanding the dynamics of laser-induced demagnetization.

II. SAMPLE GROWTH AND CHARACTERIZATION

SRO thin films were grown via pulsed laser deposition at 700 °C in 0.3 mbar of oxygen and argon (1:1) on TiO$_2$-terminated STO(111). A pressed pellet of SRO was used for the target material and the energy on the target was kept constant at 2.1 J/cm$^2$. High-pressure reflection high-energy electron diffraction (RHEED) was used to monitor the growth speed and crystallinity of the SRO film in situ. RHEED patterns and atomic force microscopy imaging confirmed the presence of smooth surfaces consisting of atomically flat terraces separated by a single unit cell step (2.2 Å in the [111] direction). X-ray diffraction indicated fully epitaxial films and x-ray reflectometry was used to verify film thickness. Bulk magnetization measurements using a SQUID magnetometer indicated a Curie temperature, $T_c$, of ~150 K. Electrical transport measurements were performed in the Van der Pauw configuration and show the residual resistance ratio to be about 10 for these films.

A. Experimental methods

In the TRMOKE technique a magnetic sample is excited by the absorption of a pump beam, resulting in a change of polarization angle, $\Delta \Theta_K(\tau)$, of a time-delayed probe beam. The ultrashort pulses from a Ti:Sapph laser are used to achieve subpicosecond time resolution. Near normal incidence, as in this experiment, $\Delta \Theta_K$ is proportional to the $\hat{z}$ component of the perturbed magnetization, $\Delta M_z$. $\Delta \Theta_K$ is measured via...
a balanced detection scheme. For additional sensitivity, the derivative of $\Delta \Theta_K(t)$ with respect to time is measured by locking into the frequency of a low-amplitude ($\sim$500-fs) fast scanning delay line in the probe beam path as time is stepped through on another delay line.

III. EXPERIMENTAL RESULTS

A. Low temperature

Figure 1 shows the time derivative of $\Delta \Theta_K$ for an 18.5-nm SRO/STO(111) sample for the 16 ps following excitation with a pump beam, for temperatures between 5 and 85 K. Clear FMR oscillations are present, generated by a sudden shift in easy axis direction upon thermal excitation by a pump beam. This motion is described by the Landau-Lifshitz-Gilbert equation with the frequency of oscillation proportional to the strength of the magnetocrystalline anisotropy field, and the damping described by the dimensionless phenomenological parameter $\alpha$. The motion appears as a decaying oscillation to TRMKE. The orientation of the anisotropy field, closer to in-plane with the sample surface in SRO/STO(111) than in SRO/STO(001), makes these oscillations more prominent when observed with the polar Kerr geometry compared to previous measurements.

Attempting to model the time derivative of $\Delta \Theta_K$ with a damped sine reveals that it cannot be fit by such a function for $t < 2$ ps. The feature at short times in Fig. 1 contains higher frequency components, whereas the oscillations which become clear after 2 ps are at a single frequency. The deviation between the measured signal and a damped sine is shown in Fig. 2.

A comparison of the amplitude of the first peak (at $t \sim 0.5$ ps) with the amplitude of the subsequent oscillations (defined as the difference in $d\Delta \Theta_K/dt$ at the peak at $\sim 3.5$ ps versus the dip at $\sim 5.5$ ps) is shown as a function of temperature in Fig. 3. The constant offset between the two amplitudes indicates that $d\Delta \Theta_K/dt$ is comprised of a superposition of a temperature-independent, short-lived component with longer-lived damped oscillations.

Fitting the oscillatory portion of the signal to a damped sine, the temperature dependencies of the amplitude, frequency, and damping parameter are found, as shown in Fig. 4. Comparing these parameters for SRO/STO(111) to previously published work on SRO/STO(001), the frequency is found to be somewhat lower and to change more with temperature. Of particular interest is $\alpha$, which is also smaller in this orientation of SRO, consistent with the more pronounced FMR oscillations. Strikingly, in both orientations there is a dip in $\alpha$ around 45 K, which is relatively stronger in SRO/STO(111). This further strengthens the link between $\alpha$ and the anomalous Hall conductivity, speculated in that paper, through near degeneracies in the band structure.

B. High temperature

By taking the time derivative of $\Delta \Theta_K$, the FMR oscillations can be followed until they disappear at elevated temperatures, at which point it becomes simpler to look at $\Delta \Theta_K$ than its time derivative. Figure 5 shows $\Delta \Theta_K$ as a function of time for the first 38 ps after excitation with the pump laser, for temperatures between 120 and 165 K. A property of a second-order phase
transitions is that the derivative of the order parameter diverges near the transition temperature. The peak in magnitude of $\Delta \Theta_K$ in Fig. 5, shown in Fig. 6, can be understood as the result of the derivative of magnetization with respect to the temperature becoming steeper near the Curie temperature. A strong temperature dependence of the demagnetization time $\tau_M$ is seen, with $\tau_M$ significantly enhanced near 150 K, consistent with previous reports on SRO.6,8

The rise time of $\Delta \Theta_K(t)$ in Fig. 5, normalized by the largest value of $\Delta \Theta_K(t)$ in the first 38 ps, can be fit with the following function:

\[
\begin{align*}
\text{for } t < 0, \quad \frac{\Delta \Theta_K(t)}{\Delta \Theta_{\text{max}}(t)} &= 0, \\
\text{and for } t > 0, \quad \frac{\Delta \Theta_K(t)}{\Delta \Theta_{\text{max}}(t)} &= C - Ae^{-t/\tau_M},
\end{align*}
\]

(1)

where the decay time is $\tau_M$. An example of these fits is shown in Fig. 7. The resulting $\tau_M$ is plotted as a function of temperature in Fig. 8. Notably, $\tau_M$ increases by a factor of 10 from 135 to 150 K. Taking the fit value of $T_c = 148.8$ K, as discussed later, $\tau_M$ is plotted log-log as a function of reduced temperature, $t_R = (T_c - T)/T_c$, in Fig. 9. The result looks approximately linear, indicating a power-law dependence of $\tau_M$ on the reduced temperature.

IV. DISCUSSION

Efforts to explain demagnetization have been largely phenomenological thus far, understandably, given the daunting challenge of a full microscopic model. Beaurepaire et al.1 introduced the three-temperature model (3TM) to describe demagnetization resulting from the interactions of the electron, phonon, and spin baths. In the 3TM the dynamics are determined by the specific heats of each bath as well as the coupling constants between them. Demagnetization can generally be described with the appropriate choice of coupling constants, providing a guide into the microscopic mechanism. Koopmans et al.10 also offer a phenomenological description of demagnetization considering three baths, but one that follows spin in addition to heat. Spin is treated as a two-state system.
with energy levels separated by an exchange gap, and Fermi’s golden rule is used to relate demagnetization to electron scattering which flips a spin. Equations for coupling strengths are derived based on parameters such as the density of states of electrons, phonons, and spins, the electron-phonon scattering rate, and the probability of spin flip at a scattering event.

In the following we attempt to understand the behavior of the demagnetization time near the transition temperature \( T_c \) with an approach based on the two-spin-state model. A general relationship between the laser-induced demagnetization time \( \tau_M \) and the spin-flip time \( \tau_{sf} \) can be derived near the transition temperature based on the concept of detailed balance. At equilibrium, the ratio of the probability of a spin flipping from majority to minority to the reverse of this process is the Boltzmann factor, \( e^{-\Delta_{ex}/kT} \), where \( \Delta_{ex} \) is the exchange energy gap. The time derivative of the number of majority and minority electrons can then be written as:

\[
\dot{N}_{maj} = -\dot{N}_{min} = \frac{N_{min}}{\tau_{sf}} - \frac{N_{maj}}{\tau_{sf}} e^{-\Delta_{ex}/kT}.
\]  

When the sample is thermally excited by a pump beam, the electron temperature \( T_e \) is increased by \( \delta T_e \). The rate of change of spins is then altered in the following way:

\[
\dot{N}_{maj} = -\dot{N}_{min} = \frac{N_{min}}{\tau_{sf}} - \frac{N_{maj}}{\tau_{sf}} e^{-\Delta_{ex}/k(T+\delta T_e)}.
\]  

The demagnetization time is related to the total change in spin polarization \( \Delta S \) from initial to final temperature, where, setting \( h=1 \), \( S \) is defined by:

\[
S(T) = \frac{1}{2} (N_{maj} - N_{min})/N_{total}.
\]  

Assuming that \( \Delta S \), as a function of time, can be written as:

\[
\Delta S(t) = (S(T_f) - S(T_i))(1 - e^{-t/\tau_M}),
\]  

the demagnetization time is given by:

\[
\tau_M = \frac{\Delta S}{\dot{S}(0)},
\]  

where \( \dot{S}(0) \) is the initial change in the time derivative of the spin polarization.

The total change in spin can be calculated by taking the derivative of \( S \) with respect to \( T \), and multiplying by \( \Delta T_{eq} \), the increase in temperature once electrons, phonons, and spins have come into thermal equilibrium with each other. \( S(T) \) and \( \Delta S \) then become:

\[
S(T) = -\frac{1}{2} \tanh \left( \frac{\Delta}{2kT} \right)
\]  

and

\[
\Delta S = \frac{dS}{dT} |_{T=T_0} \Delta T_{eq} = -\frac{\Delta_{ex}}{4kB T_0^2} \left[ T_0 \frac{\Delta'_{ex}}{\Delta_{ex}} - 1 \right] \Delta T_{eq},
\]  

where \( \Delta'_{ex} \) is the derivative of \( \Delta_{ex} \) with respect to temperature. Here we have relied on the fact that near the transition temperature, \( \Delta_{ex} \ll kB T \), and made the approximation that \( \delta T_e \ll T \) for low laser power. In the last equation \( T_0 \frac{\Delta'_{ex}}{\Delta_{ex}} \gg 1 \) near \( T_c \), so only the first term is considered.

The quantity \( \dot{S}(0) \), where \( S = 1/2(N_{maj} - N_{min})/N_{total} \), can be found by taking the derivative of \( S(0) \) with respect to \( T_e \), since immediately after excitation the electron temperature has increased, but the spin temperature \( T \) has not:

\[
\dot{S}(0) = \frac{dS}{dT_e} |_{T=T_0} \Delta T_{eq} = \frac{N_{maj}}{N_0 \tau_{sf} kB T} \Delta_{ex}. \]
Determination of the Spin-Flip Time in . . .

Taking the derivative, we find

\[ \Delta_1 / \Delta_1 = (T_c - T)^\alpha \]

where \( \Delta_1 \sim (T_c - T)^\alpha \) and \( \beta \) is the critical exponent of the order parameter. Taking the derivative, we find \( \Delta_1' \sim -\beta(T_c - T)^{\alpha-1} \) and, thus, can write

\[ \tau_M = \beta \tau_{sf} \left( \frac{T_c}{T_c - T} \right) \]

Therefore \( \tau_M \) is predicted to scale as \( 1/(T_c - T) \) near the transition temperature. A fit of \( T_c \sim 148.8 \) K is found for the data in Fig 8, Figure 9, in which \( \tau_M \) is plotted log-log as a function of the reduced temperature for this value of \( T_c \), shows the accuracy of this fit.

Note that detailed balance suggests that the demagnetization time scales as \( 1/t_R \) near the transition temperature regardless of the underlying mechanism of the demagnetization. Additionally, the critical exponent found is independent of \( \beta \). It should also be noted that the current situation, where the sample has been excited by a laser, is distinct from critical behavior as typically considered. Critical behavior relates to the time scale of fluctuations in equilibrium. Critical slowing-down is observed most directly in inelastic scattering measurements of neutrons or photons. In our experiment, not only are we perturbing the system far from equilibrium, but also we are creating disequilibrium between the different degrees of freedom. There may be a connection between the diverging time scale of equilibrium fluctuations and the time scale for returning to equilibrium after perturbation, but it cannot be assumed. \( \tau_{sf} \) is plotted as a function of temperature for the mean-field value of \( \beta = 1/2 \), which has been shown to be suitable for SRO.\(^{13} \) in Fig. 10. \( \tau_{sf} \) is revealed to be approximately 20 fs and nearly constant as a function of temperature.

Previous reports of conductivity in SRO give a scattering time of \( \sim 20 \) fs near the transition temperature.\(^{15} \) A comparison of the spin-flip time with the scattering time implies a probability of 0.1 that a scattering events results in a spin flip. Though electron-phonon interactions are the most commonly considered source of demagnetization, as mentioned previously, Eliot Yafet–like electron-electron Coulomb scattering can also result in demagnetization.\(^{5} \) This is especially true for materials with strong spin-orbit coupling, such as SRO. Additionally, in SRO the interaction with the crystal field means that total spin is not conserved,\(^{14} \) so every electron interaction can perturb the spin state.

Having found a relationship between the demagnetization time and the spin-flip time, we would like to explore the relationship between these parameters and the damping parameter \( \alpha \). It is reasonable that the damping parameter should be proportional to the spin-flip scattering rate or inversely proportional to the spin-flip scattering time: \( \alpha \sim 1/\tau_{sf} \). This can be explained as follows: Eliot-Yafet–type scattering dissipates energy from motion described by the LLG equation by disrupting the coherent, collective precession of spins. Spins that have had their angular momentum changed through electron collisions must be pulled back into the precession through the exchange interaction, representing a transfer of energy away from the precessional motion. These collision-mediated spin-orbit coupling effects are thought to be the primary source of Gilbert-type damping in ferromagnets.\(^{3} \) Again, this should be particularly true in a ferromagnet with strong spin-orbit coupling.

Combining the spin-flip time and the damping parameter with Planck’s constant, an energy scale \( \mathcal{E} \) can be defined by the condition that

\[ \frac{1}{\alpha} \equiv \frac{\mathcal{E}}{\hbar} \tau_{sf}. \]

Noting that the values for \( \alpha \) and \( \tau_{sf} \) found in Figs. 4 and 10, respectively, are approximately constant as a function of temperature, this energy scale for SRO is \( \sim 7 \) meV. The fundamental energy scales applicable to the magnetic system in SRO are the Fermi energy, the exchange energy, and the critical temperature, the latter two of which are interdependent. The Fermi energy is orders of magnitude higher than 7 meV, but the energy associated with the critical temperature, \( k_BT_c \sim 13 \) meV, is of the same order. This suggests an underlying connection among the critical temperature (and thus the exchange energy), Gilbert damping, and spin-flip scattering.

A relationship similar to Eq. (12) has been found previously between \( \tau_M \) (rather than \( \tau_{sf} \)) and \( \alpha \) by Koopmans et al.\(^{10} \) at low temperature:

\[ \tau_M = \frac{1}{4} \frac{\hbar}{k_B} \frac{1}{T_c} \frac{1}{\alpha}. \]

Applying this equation to SRO at 5 K yields \( \tau_M \sim 30 \) fs, which is unphysical since it is below the total scattering rate of \( \sim 100 \) fs at low temperature.\(^{15} \) Whether the fundamental relationship is between the transition temperature and the demagnetization time or the spin-flip scattering time remains a question for a microscopic model to resolve.

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